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MM      MM      TTTTTTTTTT  HH      HH      HH      HH      CCCCCCCC  000000  SSSSSSSS  HH      HH
MM      MM      TTTTTTTTTT  HH      HH      HH      HH      CCCCCCCC  000000  SSSSSSSS  HH      HH
MMMM    MMMM      TT      HH      HH      HH      HH      CC      00      00      SS      HH      HH
MMMM    MMMM      TT      HH      HH      HH      HH      CC      00      00      SS      HH      HH
MM      MM      TT      HH      HH      HH      HH      CC      00      00      SS      HH      HH
MM      MM      TT      HH      HH      HH      HH      CC      00      00      SS      HH      HH
MM      MM      TT      HHHHHHHHHH  HHHHHHHHHH  CC      00      00      SSSSSS  HHHHHHHHHH
MM      MM      TT      HHHHHHHHHH  HHHHHHHHHH  CC      00      00      SSSSSS  HHHHHHHHHH
MM      MM      TT      HH      HH      HH      HH      CC      00      00      SS      HH      HH
MM      MM      TT      HH      HH      HH      HH      CC      00      00      SS      HH      HH
MM      MM      TT      HH      HH      HH      HH      CC      00      00      SS      HH      HH
MM      MM      TT      HH      HH      HH      HH      CC      00      00      SS      HH      HH
MM      MM      TT      HH      HH      HH      HH      CCCCCCCC  000000  SSSSSSSS  HH      HH
MM      MM      TT      HH      HH      HH      HH      CCCCCCCC  000000  SSSSSSSS  HH      HH
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LL      IIIIII  SSSSSSSS
LL      IIIIII  SSSSSSSS
LL      II      SS
LL      II      SS
LL      II      SS
LL      II      SS
LL      II      SSSSSS
LL      II      SSSSSS
LL      II      SS
LL      II      SS
LL      II      SS
LL      II      SS
LLLLLLLLLL  IIIIII  SSSSSSSS
LLLLLLLLLL  IIIIII  SSSSSSSS
```


(2) 50
(3) 72
(4) 152

HISTORY ; Detailed Current Edit History
DECLARATIONS ; Declarative Part of Module
MTH\$HCOSH - H Floating point COSH function


```
0000 1 .TITLE MTH$HCOSH ; H floating Hyperbolic Cosine routine
0000 2 ; (HCOSH)
0000 3 .IDENT /1-006/ ; File: MTHHCOSH.MAR EDIT: RNH1006
0000 4 ;
0000 5 ;*****
0000 6 ;
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0000 23 ; SOFTWARE ON EQUIPMENT WHICH IS NOT SUPPLIED BY DIGITAL.
0000 24 ;
0000 25 ;*****
0000 26 ;
0000 27 ;
0000 28 ;
0000 29 ; FACILITY: MATH LIBRARY
0000 30 ;++
0000 31 ; ABSTRACT:
0000 32 ;
0000 33 ; MTH$HCOSH is a function which returns the H floating hyperbolic cosine
0000 34 ; of its H floating point argument. The call is standard
0000 35 ; call-by-reference.
0000 36 ;
0000 37 ;--
0000 38 ;
0000 39 ; VERSION: 1
0000 40 ;
0000 41 ; HISTORY:
0000 42 ; AUTHOR:
0000 43 ; John A. Wheeler, 12-Sep-1979: Version 1
0000 44 ;
0000 45 ; MODIFIED BY:
0000 46 ;
0000 47 ;
0000 48 ;
```


MTH\$HCOSH
1-006

E 15
; H floating Hyperbolic Cosine routine 16-SEP-1984 01:35:02 VAX/VMS Macro V04-00
HISTORY ; Detailed Current Edit History 6-SEP-1984 11:24:49 [MTHRTL.SRC]MTHHCOSH.MAR;1

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(2)

```
0000 50      .SBTTL  HISTGRY ; Detailed Current Edit History
0000 51
0000 52
0000 53 ; Edit History for Version 1 of MTH$HCOSH
0000 54
0000 55 : 1-001 - Adapted from MTH$GCOSH.  JW 12-Sep-1979
0000 56 : 1-002 - Use MTH$HEXP R6.  SBL 4-Oct-1979
0000 57 : 1-003 - H_0.25 should be literal rather than own storage.  SBL 7-Oct-1979
0000 58 : 1-004 - Don't store reserved operand before signal.  SBL 7-Feb-1980
0000 59 : 1-005 - Changed lower limit for Chebyshev approximation from 2**-56 to
0000 60 : 2**-57.
0000 61 : - Eliminated second call to EXP for input values between .25 and
0000 62 : 57*ln2 by computing COSH(x) = (Z + 1/Z)/2, with Z = EXP(ixi).
0000 63 : - Eliminated second call to EXP for input values between 57*ln2
0000 64 : and 16383*ln2.
0000 65 : - Changed all final floating point divisions by 2 to interger
0000 66 : subtracts of 1 from the exponent field.
0000 67 : - Extended maximum range to 16384*ln2.
0000 68 : - Changed logic for computing EXP(ixi-ln2) to reduce error.
0000 69 : - RNH 10-FEB-81
0000 70 : 1-006 - Eliminated symbolic short literals.  RNH 15-Oct-81
```



```
0000 72      .SBTTL  DECLARATIONS      ; Declarative Part of Module
0000 73
0000 74      ;
0000 75      ; INCLUDE FILES:
0000 76      ;
0000 77      ; EXTERNAL SYMBOLS:
0000 78      .DSABL  GBL
0000 79      .EXTRN  MTH$$SIGNAL
0000 80      .EXTRN  MTH$K_FLOOVEMAT
0000 81      .EXTRN  MTH$HEXP_R6
0000 82      ;
0000 83      ; EQUATED SYMBOLS:
0000 84
0000 85
0000 86      ;
0000 87      ; MACROS:      none
0000 88      ;
0000 89
0000 90
0000 91      ;
0000 92      ; PSECT DECLARATIONS:
0000 93
00000000 94      .PSECT  _MTH$CODE      PIC,SHR, LONG, EXE, NOWRT
0000 95      ; program section for math routines
0000 96      ;
0000 97      ; OWN STORAGE:  none
0000 98      ;
0000 99      ;
0000 100     ; CONSTANTS:
0000 101     ;
0000 102     ;
0000 103     H_16383_LOG_2:
0000 104     .QUAD  ^XE3E0A45E62DE400E
0000 105     .QUAD  ^X6B251812C66964DB      ; 16383*ln2
0010 106     H_16384_LOG_2:
0010 107     .QUAD  ^XA39E2FEF62E4400E
0018 108     .QUAD  ^X07E6673093C7F357      ; 16384*ln2
0020 109     H_LOG_2_HI:
0020 110     .QUAD  ^XA39E2FEF62E44000
0028 111     .QUAD  ^X4000673093C7F357      ; (high 109 bits of ln2)+2*-109
0030 112     H_LOG_2_LO:
0030 113     .QUAD  ^XF0CB950BC0D0BF9D
0038 114     .QUAD  ^X5F359D27D674CD98      ; ln2 - H_LOG_2_HI
0040 115     H_2_POWER_57:
0040 116     .QUAD  ^X0000000000000403A
0048 117     .QUAD  0      ; 2*57
0050 118
0050 119     HCOSHTAB:
0050 120     .LONG  ^X8C8F3FAB, ^X2B3EE172      ; 2.502658279567823990162458156254711E -27
0058 121     .LONG  ^X5BD2E986, ^XADEB4F57
0060 122     .LONG  ^XF2C93FB1, ^XD01949AF      ; 1.611665395066462480330719767236559E -24
0068 123     .LONG  ^X1DF63B8C, ^XC60346B9
0070 124     .LONG  ^X0CE33FBB, ^X64FF997D      ; 8.896792721476872237647982378253568E -22
0078 125     .LONG  ^X0B3F40F3, ^X7CB38AA4
0080 126     .LONG  ^XE5423FC3, ^XF4FDBA3C      ; 4.110317621712466937445902717251860E -19
0088 127     .LONG  ^X6DEFA6F1, ^X60105113
0090 128     .LONG  ^X68273FCC, ^X9928863B      ; 1.561920696859944528721805191130865E -16
```


E533A92E	54A49ACF	0098	129	.LONG	^X54A49ACF, ^XE533A92E	
3B813E73	AE7F3FD4	00A0	130	.LONG	^XAE7F3FD4, ^X3B813E73	; 4.779477332387377634901255174808471E -14
4B6B3FDC	D10B2ED8	00A8	131	.LONG	^XD10B2ED8, ^X4B6B3FDC	
07C94A8C	93973FDC	00B0	132	.LONG	^X93973FDC, ^X07C94A8C	; 1.147074559772972474513234083768590E -11
7DE98CBB	FC3DD25A	00B8	133	.LONG	^XFC3DD25A, ^X7DE98CBB	
8D898EFF	1EED3FE4	00C0	134	.LONG	^X1EED3FE4, ^X8D898EFF	; 2.087675698786809897912112497212423E -9
85215944	371B7B54	00C8	135	.LONG	^X371B7B54, ^X85215944	
89F5FB77	27E43FEB	00D0	136	.LONG	^X27E43FEB, ^X89F5FB77	; 2.755731922398589065255749092851911E -7
94EA88C4	F01FC72E	00D8	137	.LONG	^XF01FC72E, ^X94EA88C4	
1A0101A0	A01A3FF1	00E0	138	.LONG	^XA01A3FF1, ^X1A0101A0	; 2.480158730158730158730158708693922E -5
1BE015A7	01A0A01A	00E8	139	.LONG	^X01A0A01A, ^X1BE015A7	
16C1C16C	6C163FF7	00F0	140	.LONG	^X6C163FF7, ^X16C1C16C	; 1.3888888888888888888888888888904959E -3
B9DF16C2	C16C6C16	00F8	141	.LONG	^XC16C6C16, ^XB9DF16C2	
55555555	55553FFC	0100	142	.LONG	^X55553FFC, ^X55555555	; 4.166666666666666666666666666666666603E -2
54ED5555	55555555	0108	143	.LONG	^X55555555, ^X54ED5555	
00000000	00004000	0110	144	.LONG	^X00004000, ^X00000000	; 5.000000000000000000000000000000000000E -1
00000000	00000000	0118	145	.LONG	^X00000000, ^X00000000	
00000000	00004001	0120	146	.LONG	^X00004001, ^X00000000	; 9.999999999999999999999999999999999999E -1
00000000	00000000	0128	147	.LONG	^X00000000, ^X00000000	
		0130	148			
0000000E		0130	149	HCOSHLEN	= .- HCOSHTAB/16	
		0130	150			

```
0130 152      .SBTTL MTH$HCOSH - H Floating point COSH function
0130 153
0130 154
0130 155 :++
0130 156 : FUNCTIONAL DESCRIPTION:
0130 157
0130 158 : HCOSH - double precision H floating point function
0130 159
0130 160 : HCOSH(X) is computed as:
0130 161
0130 162 :       If |X| < 2*-57, HCOSH(X) = 1.
0130 163 :       If 2*-57 <= |X| < 0.25, HCOSH(X) = Chebyshev series
0130 164 :       If 0.25 <= |X| < 57*ln2, let Z = HEXP(|X|) and set HCOSH(X) = (Z+1/Z)/2
0130 165 :       If 57*ln2 <= |X| < 16383*ln2, then HCOSH(X) = HEXP(|X|)/2.
0130 166 :       If 16383*ln2 <= |X| < 16384*ln2, then HCOSH(X) = HEXP(|X|-ln2).
0130 167 :       If 16384*ln2 <= |X|, then overflow.
0130 168
0130 169 : CALLING SEQUENCE:
0130 170
0130 171 :       hcosh.wh.v = MTH$HCOSH(x.rh.r)
0130 172
0130 173 :       -or-
0130 174
0130 175 :       CALL MTH$HCOSH(hcosh.wh.r, x.rh.r)
0130 176
0130 177 :       Because an H-floating result cannot be expressed in 64 bits, it is
0130 178 :       returned as the first argument, with the input parameter displaced
0130 179 :       to the second argument, in accordance with the Procedure Calling
0130 180
0130 181 : INPUT PARAMETERS:
0130 182
0130 183 :
00000004 0130 184 :       LONG = 4 ; define longword multiplier
00000008 0130 185 :       x = 2 * LONG ; Contents of x is the argument
0130 186
0130 187 : IMPLICIT INPUTS: none
0130 188
0130 189 : OUTPUT PARAMETERS:
0130 190
00000004 0130 191 :       hcosh = 1 * LONG
0130 192
0130 193 : IMPLICIT OUTPUTS: none
0130 194
0130 195 : COMPLETION CODES: none
0130 196
0130 197 : SIDE EFFECTS:
0130 198
0130 199 : Signal: MTH$ FLOOVEMAT if 16384*ln2 <= |X| with reserved operand in R0/R3
0130 200 : (copied to the signal mechanism vector CHF$MCH_R0/R1 by LIB$SIGNAL).
0130 201 : Associated message is: "FLOATING OVERFLOW IN MATH LIBRARY". Result is reserved
0130 202 : operand -0.0 unless a user supplied (or any) error handler changes CHF$MCH_R0/R1
0130 203
0130 204 : NOTE: This procedure disables floating point underflow, enables integer
0130 205 : overflow.
0130 206
0130 207 : ---
0130 208
```



```

                                0130 209
                                40FC 0130 210      .ENTRY MTH$HCOSH, ^M<IV, R2, R3, R4, R5, R6, R7 >
                                0132 211      ; standard call-by-reference entry
                                0132 212      ; disable DV (and FU), enable IV
                                0132 213      MTH$FLAG_JACKET      ; flag that this is a jacket procedure in
                                0132
                                6D 00000000'GF 9E 0132      MOVAB G^MTH$$JACKET_HND, (FP)
                                0139      ; set handler address to jacket
                                0139      ; handler
                                0139
                                6D 00000000'GF 9E 0139 214      MOVAB G^MTH$$JACKET_HND, (FP)      ; case of an error in routine
                                0139 215      ; Set handler address to jacket handler
                                0140 216      ; If an error, convert signal to user PC
                                0140 217      ; and resignal
                                50 08 BC 70FD 0140 218      MOVH @x(AP), R0      ; R0/R3 = |X| = @value(AP)
                                50 8000 8F AA 0145 219      BICW2 #^X8000, R0      ; R0/R3 = |X|
                                3FFF 8F 50 B1 014A 220      CMPW R0, #^X3FFF      ; compare |X| with 0.25
                                1E 18 014F 221      BGEQ GEQ_TO_0.25      ; branch if |X| >= 0.25
                                0151 222
                                0151 223      ;
                                0151 224      ; |X| < 0.25
                                0151 225      ;
                                0151 226
                                3FC8 8F 50 B1 0151 227      CMPW R0, #^X3FC8      ; compare |X| with 2*-57
                                06 18 0156 228      BGEQ GEQ_TO_2M57      ; branch if |X| >= 2*-57
                                0158 229
                                0158 230      ;
                                0158 231      ; |X| < 2*-57
                                0158 232      ;
                                0158 233
                                04 BC 08 70FD 0158 234      MOVH #1, @hcosh(AP)      ; Store 1.0 as result
                                04 04 015D 235      RET      ; return
                                015E 236
                                015E 237      ;
                                015E 238      ; 2*-57 <= |X| < 0.25
                                015E 239      ;
                                015E 240
                                015E 241      GEQ_TO_2M57:
                                FEE7 CF 50 50 64FD 015E 242      MULH2 R0, R0      ; Get ARG*2 for POLYH.
                                50 75FD 0162 243      POLYH R0, #HCOSHLLEN-1, HCOSHTAB      ; R0/R3 = SUM(Ci*X^i)
                                04 BC 50 70FD 0169 244      MOVH R0, @hcosh(AP)      ; Store result in first argument
                                04 04 016E 245      RET      ; return
                                016F 246
                                016F 247      ;
                                016F 248      ; 0.25 <= |X|
                                016F 249      ;
                                016F 250      ;
                                016F 251
                                016F 252      GEQ_TO_0.25:
                                FE8B CF 50 71FD 016F 253      CMPL R0, H 16383 LOG_2      ; compare |X| with 16383*ln2
                                20 14 0175 254      BGTR GTR_TRAN_16383_LOG_2      ; branch if |X| > 16383*ln2
                                0177 255
                                0177 256      ;
                                0177 257      ; 0.25 <= |X| <= 16383*ln2
                                0177 258      ;
                                0177 259
                                00000000'EF 16 0177 260      JSB MTH$HEXP_R6      ; R0/R3 = HEXP(|X|)
```

```
FEBD CF 50 71FD 017D 261 CMPH R0, H_2 POWER_57 ; Compare HEXP(!X!) with 2*57, if
09 14 0183 262 BGTR ONE_TERM_ONLY- ; larger, only one term is needed.
54 08 50 67FD 0185 263 DIVH3 R0, #1, R4 ; R4/R7 = HEXP(-!X!)
50 54 60FD 018A 264 ADDH2 R4, R0 ; R0/R3 = HEXP(X) + HEXP(-X)
018E 265 ONE_TERM_ONLY:
018E 266 SUBW2 #^X0001, R0 ; R0/R3 = (HEXP(X) + HEXP(-X))/2
04 BC 50 7DFD 0191 267 MOVO R0, @hcosh(AP) ; move COSH(x) to first argument
04 0196 268 RET ; and return
0197 269
0197 270 ;
0197 271 ; 16383*ln2 < !X!
0197 272 ;
0197 273 ;
0197 274 GTR_THAN 16383_LOG_2:
FE73 CF 50 71FD 0197 275 CMPH R0, H_16384_LOG_2 ; compare !X! with 16384*ln2
1A 18 019D 276 BGEQ ERROR ; branch to ERROR if 16384*ln2 <= !X!
019F 277
019F 278
019F 279 ;
019F 280 ; 16383*ln2 <= !X! < 16384*ln2
019F 281 ;
019F 282 ;
50 FE7C CF 62FD 019F 283 SUBH2 H_LOG_2_HI, R0 ; R0/R3=!X!-(hi 109 bits of ln2+2*-109)
00000000'EF 16 01A5 284 JSB MTH$HEXP_R6 ; R0/R3=HEXP(!X!-H_LOG_2_HI)
54 50 FE80 CF 65FD 01AB 285 MULH3 H_LOG_2_LO, R0, R4 ; R4/R7=H_LOG_2_LO*HEXP(!X!-H_LOG_2_LO)
04 BC 50 54 61FD 01B2 286 ADDH3 R4, R0, @hcosh(AP) ; Store HEXP(!X!-ln2) in 1st argument
04 01B8 287 RET ; return
01B9 288
01B9 289 ;
01B9 290 ; 16383*ln2 + LOG(2) <= !X!, error
01B9 291 ;
01B9 292 ;
7E 00'8F 9A 01B9 293 ERROR: MOVZBL #MTH$K_FLOOVEMAT, -(SP) ; condition value
50 01 0F 79 01BD 294 ASHQ #15, #T, R0 ; R0 = result = reserved operand -0.0
01C1 295 ; goes to R0/R3 so error handler
01C1 296 ; can modify the result.
00000000'EF 52 7C 01C1 297 CLRQ R2 ;
04 BC 01 01 FB 01C3 298 CALLS #1, MTH$$SIGNAL ; signal error and use real user's PC
04 50 7DFD 01CA 299 MOVO R0, @hcosh(AP) ; Restore result
01CF 300 RET ; return
01D0 301
01D0 302
01D0 303
01D0 304 .END
```


MTH\$HCOSH
Symbol table

K 15
; H floating Hyperbolic Cosine routine

16-SEP-1984 01:35:02
6-SEP-1984 11:24:49

VAX/VMS Macro V04-00
[MTHRTL.SRC]MTHHCOSH.MAR;1

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```
ERROR          000001B9 R    01
GEQ_TO_0.25    0000016F R    01
GEQ_TO_2M57    0000015E R    01
GTR_THAN_16383_LOG_2 00000197 R    01
HCOSH          = 00000004
HCOSHLEN       = 0000000E
HCOSHTAB       00000050 R    01
H_16383_LOG_2  00000000 R    01
H_16384_LOG_2  00000010 R    01
H_2_POWER_57   00000040 R    01
H_LOG_2_HI     00000020 R    01
H_LOG_2_LO     00000030 R    01
LONG          = 00000004
MTH$$JACKET_HND ***** X    01
MTH$$SIGNAL    ***** X    00
MTH$HCOSH      00000130 RG   01
MTH$HEXP_R6    ***** X    00
MTH$K_FLOOVEMAT ***** X    00
ONE_TERM_ONLY  0000018E R    01
X              = 00000008
```

+-----+
! Psect synopsis !
+-----+

PSECT name	Allocation	PSECT No.	Attributes
ABS	00000000 (0.)	00 (0.)	NOPIC USR
MTH\$CODE	000001D0 (464.)	01 (1.)	PIC USR

CON ABS LCL NOSHR NOEXE NORD NOWRT NOVEC BYTE
CON REL LCL SHR EXE RD NOWRT NOVEC LONG

+-----+
! Performance indicators !
+-----+

Phase	Page faults	CPU Time	Elapsed Time
Initialization	32	00:00:00.07	00:00:01.11
Command processing	126	00:00:00.68	00:00:03.06
Pass 1	91	00:00:01.06	00:00:04.74
Symbol table sort	0	00:00:00.00	00:00:00.00
Pass 2	66	00:00:00.78	00:00:02.77
Symbol table output	4	00:00:00.02	00:00:00.02
Psect synopsis output	3	00:00:00.02	00:00:00.12
Cross-reference output	0	00:00:00.00	00:00:00.00
Assembler run totals	324	00:00:02.64	00:00:11.85

The working set limit was 900 pages.
4622 bytes (10 pages) of virtual memory were used to buffer the intermediate code.
There were 10 pages of symbol table space allocated to hold 20 non-local and 0 local symbols.
364 source lines were read in Pass 1, producing 11 object records in Pass 2.
1 page of virtual memory was used to define 1 macro.

MTH\$HCOSH
VAX-11 Macro Run Statistics

L 15
; H floating Hyperbolic Cosine routine

16-SEP-1984 01:35:02
6-SEP-1984 11:24:49

VAX/VMS Macro V04-00
[MTHRTL.SRC]MTHHCOSH.MAR;1

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+-----+
! Macro library statistics !
+-----+

Macro library name

Macros defined

_ \$255\$DUA28:[SYSLIB]STARLET.MLB;2

0

0 GETS were required to define 0 macros.

There were no errors, warnings or information messages.

MACRO/ENABLE=SUPPRESSION/DISABLE=(GLOBAL,TRACEBACK)/LIS=LIS\$:MTHHCOSH/OBJ=OBJ\$:MTHHCOSH MSRC\$:MTHJACKET/UPDATE=(ENH\$:MTHJACKET)+MSRC

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